

TESSELLATE 2024

Email: <u>tessellate@cmi.ac.in</u> Chennai Mathematical Institute, H1, SIPCOT IT Park, Siruseri, Kelambakkam, Chennai – 603103

STEMS 2025

Mathematics Syllabus

Section A

- Combinatorics
 - Basic Counting (Rule of Sum, Rule of Product, Combinations, Permutations, Principle of Inclusion-Exclusion)
 - Pigeonhole Principle
 - Induction and Proof by Contradiction
 - o Elementary Recurrence Relations and Characteristic Equations
 - Generating Functions and Binomial Theorem
 - Elementary Properties of Graphs
- Algebra
 - Linear Equations, Quadratic Equations
 - Polynomials over Z, Q, R or C.
 - o Classical Inequalities (AM-GM, Cauchy-Schwartz, Rearrangement, Schur's Inequality)
 - o Exponents, Logarithms and Trigonometric Functions
 - Complex Numbers (De-Moivre, Polar Coordinates, Conjugates, and basic properties)
 - Sequence and Series (Arithmetic Progressions, Geometric Progression, Harmonic Progression etc.)
- Geometry
 - o Euclidean Geometry (Triangle Geometry, Cyclic Quadrilaterals, Radical
 - Axis, Geometric Transformations)
 - o Coordinate Geometry (Distance Formula, Equations of Straight Lines, Equation of Circles)
 - Trigonometry (Basic properties of trigonometric functions, identities)
- Number Theory
 - o Divisibility
 - Modular Congruences (Euler's Theorem, Fermat's Little Theorem, Wilson's Theorem, Chinese Remainder Theorem may be helpful.)
 - Arithmetic Functions (Totient, Divisor, Sum of Divisors, Mobius Function)
 - Diophantine Equations
- Set Theory
 - Basics of Set Theory (Set union, intersection, symmetric difference)
 - o Relations
 - Functions
- Probability
 - o Basics of Probability (Conditional Probability, Bayes' Theorem, Binomial Trials, Expected Value)

Section B

In addition to the syllabus of section A, the following topics -

- Calculus
 - Limits and Derivatives
 - o Continuity and Differentiability
 - o Applications of Derivatives
 - Integrals, Applications of Integrals
 - Differential Equations
- Algebra
 - Inverse Trigonometric Functions
 - Vector Algebra
- Geometry
 - Coordinate Geometry (Equations of Conic Sections)
 - Three Dimensional Geometry
- Probability
 - o Basics of Linearity of Expectation

Section C

- Advanced knowledge of all concepts mentioned in the high school syllabus.
- Linear Algebra
 - Matrices
 - Linear Transformations
 - o Eigenvalues and Eigenvectors
 - o Diagonalization
 - Jordan Normal Form
- Calculus and Real Analysis
- Abstract Algebra
 - Group Theory (Basics, Cauchy and Sylow Theorems, Cayley's Theorems, Permutations, Isomorphism Theorems)
- Probability Theory
 - Probability Density Function
 - Probability Distribution Function (Bernoulli Distribution, Binomial Distribution, Poisson Distribution, Normal Distribution, Uniform Distribution, etc.)
 - o Mean and Variance
 - o Joint Probability Distribution